

Use the Auxiliary Projection Method to Solve Problems in Geometry

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Abstract - Geometry is a science with very wide applications in life. Everything around us is geometric shapes. Solving geometry problems helps us solve many real-life problems. In geometry there are many complex problems. But if a solution is found, many difficult problems will be solved quickly and easily. This article presents the auxiliary projection method to solve many problems in geometry. The following data can be determined.

Keywords: Bisecting plane 1: Pg1, Bisecting plane 2: Pg2, Front plane of projection: π_1 , Top plane of projection: π_2 .

I. INTRODUCTION

Solved by projecting the image onto the projection plane and solving the problem on its projection. Then from the results on the projection we will infer the results in space.

This method demonstrates how to select a new projection direction and a new projection plane and project the image onto the new projection plane. Solve the problems with new projections. Then convert this result to the old projection.

In addition to the basic projection planes, we can choose bisector planes.

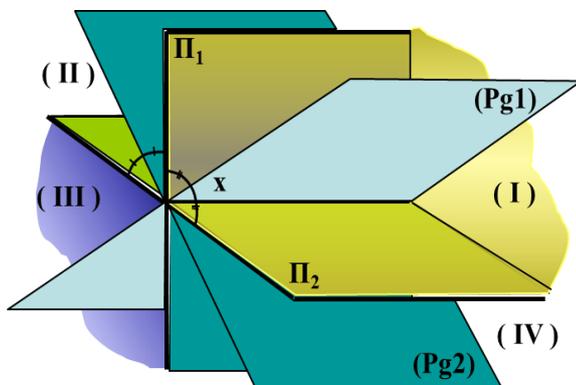


Figure 1: Some planes of projection

The points are on two bisector planes are equidistant from the π_1 and the π_2 .

The property of the Pg1 is that two projections of an object on this plane are symmetrical about the x axis (see figure 2 a and b).

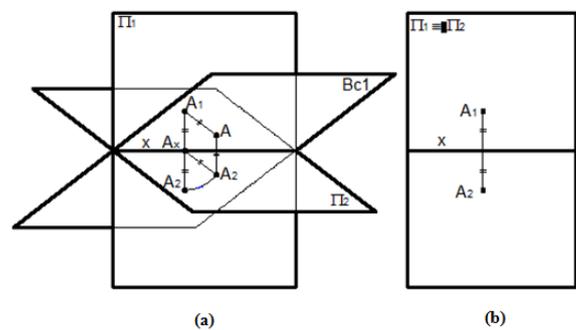


Figure 2: Properties of the Pg1

The property of the Pg2 is that two projections of an object on this plane coincide (see figure 3 a and b).

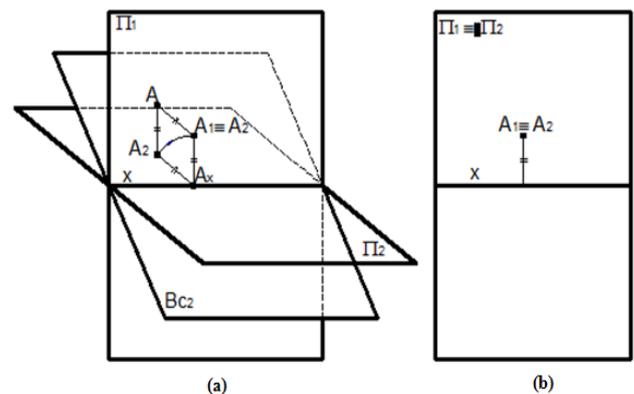


Figure 3: Properties of the Pg2

II. APPLICATION TO SOLVE SOME GEOMETRIC PROBLEMS

Problem 1: Draw the intersection of the plane ABC and profile line EF.

We project both plane ABC and EF onto the Pg2. The new projection direction is AB. The new projection of plane ABC is a line. This line intersects line E'F' at point H'. We project H' onto the π_1 and the π_2 we obtained H1 and H2. (See fig 4)

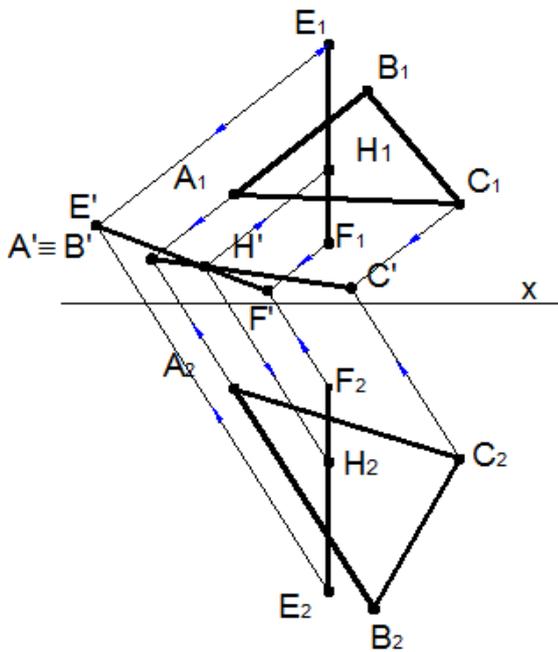


Figure 4: The intersection of a line and a plane

Problem 2: Draw the intersection of two figure planes ABC and DEF.

We project both plane ABC and DEF onto the Pg_2 . The new projection direction is EF. The new projection of plane DEF is a line. The new projection of the intersection of the two figure planes coincides with this line. Projecting this intersection line in opposite directions onto the π_1 and the π_2 we obtained two straight lines G_1H_1 and G_2H_2 . These are two projections of the intersection of two given figure planes (See fig 5).

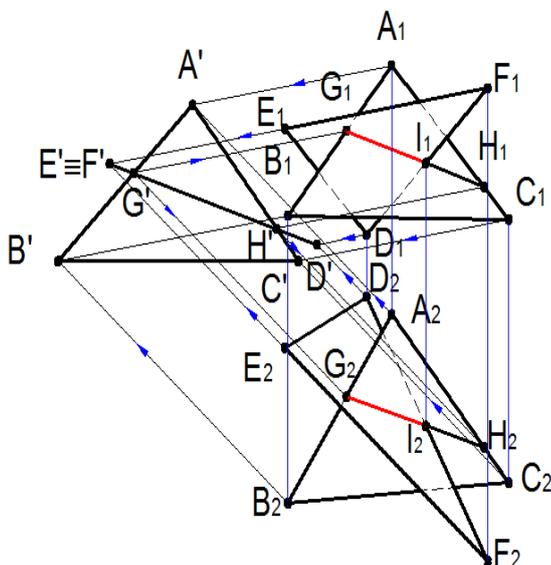


Figure 5: The intersection of two figure plane

Problem 3: Draw the intersection of line d and the prism $ABCA'B'C'$ (See figure 6).

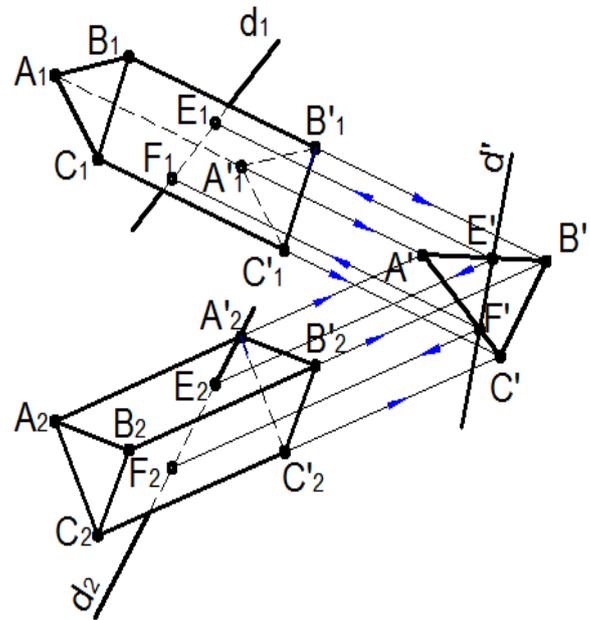


Figure 6: The intersection of a line and a prism

We project both the prism $ABCA'B'C'$ and line d onto the Pg_2 . The new projection direction is AA' . The new projection of the prism is a triangle. The new projection of line d is line d' . We will find the intersection of line d with the prism on the new projection as two points E' and F' . Projecting E' and F' in opposite directions onto the π_1 and the π_2 we obtained E_1F_1 and E_2F_2 .

Problem 4: Given two skew lines b and d. Find points on line d and a distance r from line b.

The points to be found will lie on a right circular cylinder whose axis is line b and radius r. So it is the intersection of line d with the cylinder. (See figure 7)

If line d intersects the cylinder, the problem has 2 geometric solutions.

If line d is tangent to the cylinder then the problem has a geometric solution.

If line d is neither tangent to nor intersects the right circle cylinder then the problem has no solution.

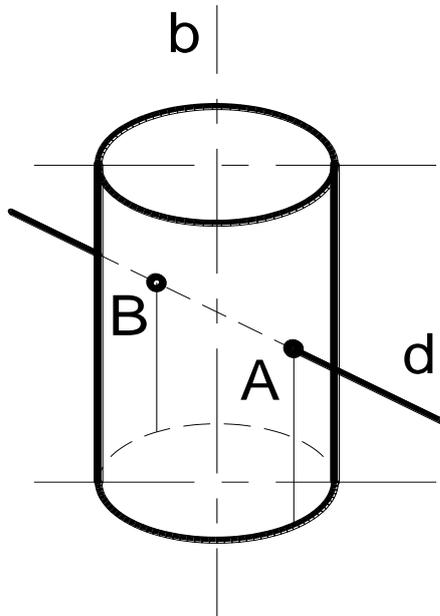


Figure 7: The intersection of a line and a cylinder

Project both lines a and d onto the π_2 in the direction of projection which is line b . The new projection of b is a point. The new projection of the cylinder is a circle. Its center is the new projection of b . This circle has radius r . The new projection of line d is a straight line d' .

If d' intersects the circle, the problem has 2 geometric solutions.

If d' is tangent to the circle, the problem has 1 solution.

If line d' is neither tangent to nor intersects the circle then the problem has no solution. (See figure 8)

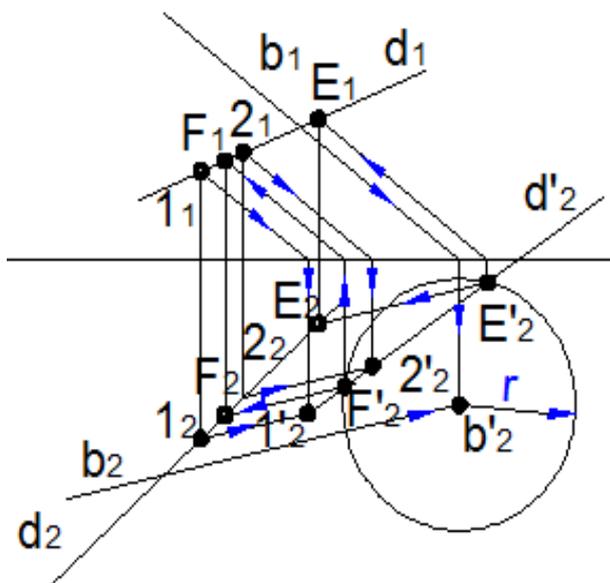


Figure 8: The intersection of a line and a cylinder

Problem 5: Given three skew lines a , b and c . Draw a straight line t intersecting the above three lines at 3 points A , B , C so that $AB=AC$.

To solve this problem, we project all three lines onto the Pg_2 in the direction of line a . We obtained a new projection.

Draw a straight line passing through A' parallel to b' , intersecting c' at E' . Line c' intersects line b' at point E' . Draw a half circle with center O' passing through E' cutting b' at C' . Join C' to A' , cut b' at B' . Then project back to the original projection (see figure 9).

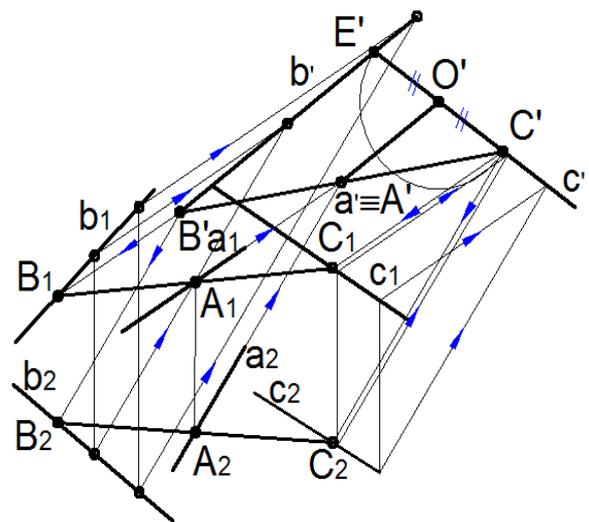


Figure 9: A line intersects 3 skew lines

Problem 6: Given two skew lines a and b .

Draw the horizontal line MN , $M \in a$, $N \in b$, $MN=d$ (see figure 10).

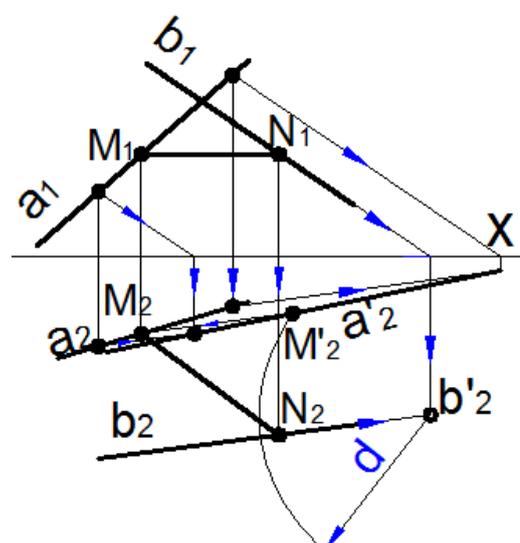


Figure 10: Draw horizontal line MN

We project two lines a and b onto the $Pg\ 2$ in the direction of line b . We obtained a new projection. Projection of line b is a point $b'2$ and projection of line a is line $a'2$. Draw a circle with center $b'2$ and radius equal to d , cutting $a'2$ at $M'2$. From $M'2$ we infer $M2$. From $M2$, infer $M1$. Draw a line passes through point $M1$ and parallel to x axis. This line intersects $b1$ at $N1$.

III. CONCLUSION

Geometry is a science that is widely applied in engineering and life. It is very complicated and there are many ways to solve it. To solve geometric problems, we must think for ourselves and find solutions. So writing articles about this subject is very difficult. Because it has no experiments, there are no cited experimental data. This article presents a new solution to solve some geometric problems. It helps us solve faster and easier to understand.

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